

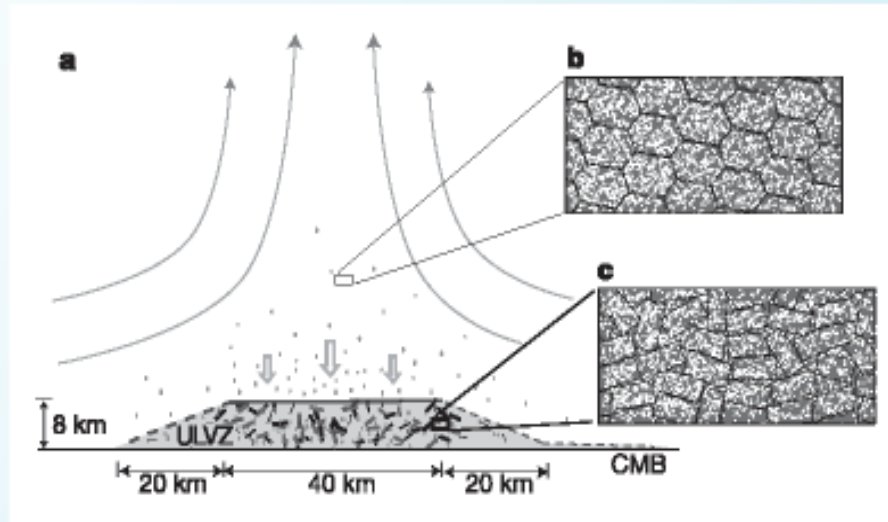
LETTERS

A crystallizing dense magma ocean at the base of the Earth's mantle

S. Labrosse¹, J. W. Hernlund² & N. Coltice^{1,3}

¹Laboratoire des sciences de la Terre, Ecole Normale Supérieure de Lyon, Université de Lyon, CNRS UMR 5570, 46 Allée d'Italie, 69364 Lyon Cedex 07, France. ²Équipe de Dynamique des Fluides Géologiques, Institut de Physique du Globe de Paris, 4 place Jussieu, 75252 Paris Cedex 05, France. ³Laboratoire des sciences de la Terre, Université Lyon 1, Université de Lyon, CNRS UMR 5570, 2 rue Raphaël Dubois, 69622 Villeurbanne Cedex, France. { Present address: Department of Earth and Ocean Sciences, University of British Columbia, Vancouver, BC V6T 1Z4, Canada.

Partial melting at the core mantle boundary

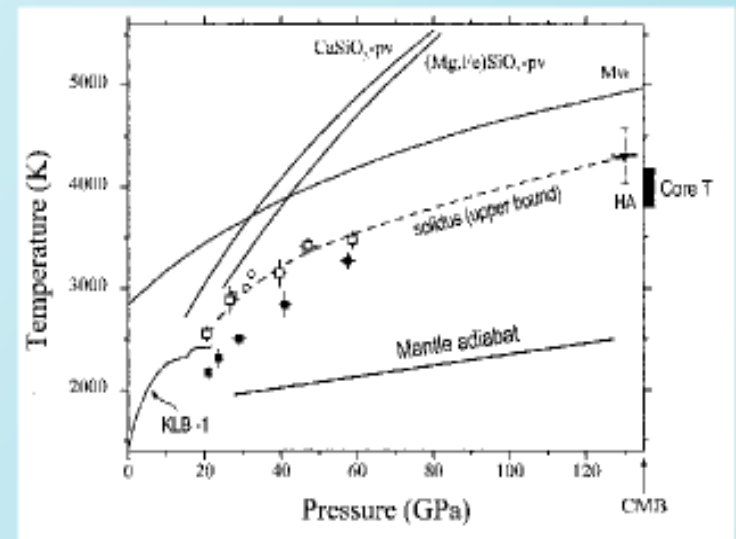


Detection of an ultra low velocity zone (ULVZ) at the plume root

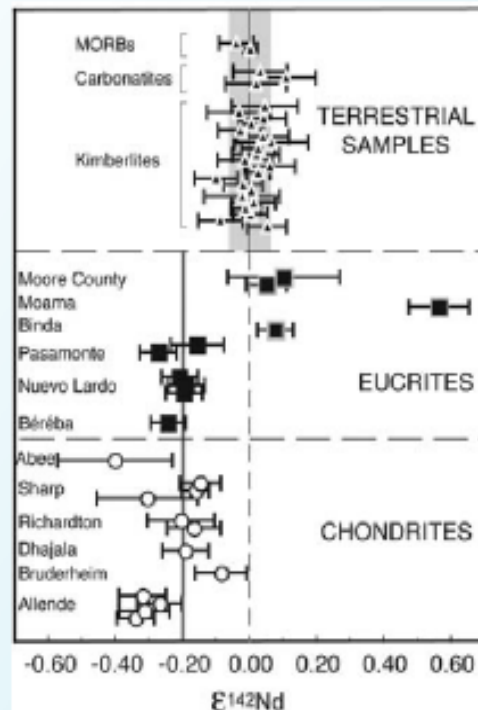
From Rost et al, 2005, Nature, **435**, 666.

Partial melting temperature of pyrolitic-like mixture

From Zerr et al, 1998, Science, **281**, 243



Early Earth differentiation



Radiogenic system ^{146}Sm - ^{142}Nd : $\tau=102$ Ma

Lithophile element : tracers of mantle differentiation (inert concerning core formation)

Existence of an hidden enriched reservoir !!!

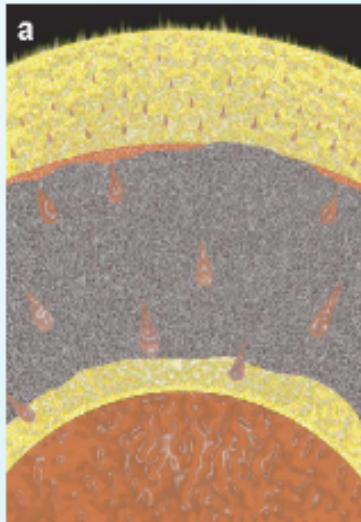
20-30% of very incompatible elements (U, Th, K, ...)

20-60% of ^{40}Ar total budget

From Boyet et al, Science, 2005, **309**, 576

Magma ocean model

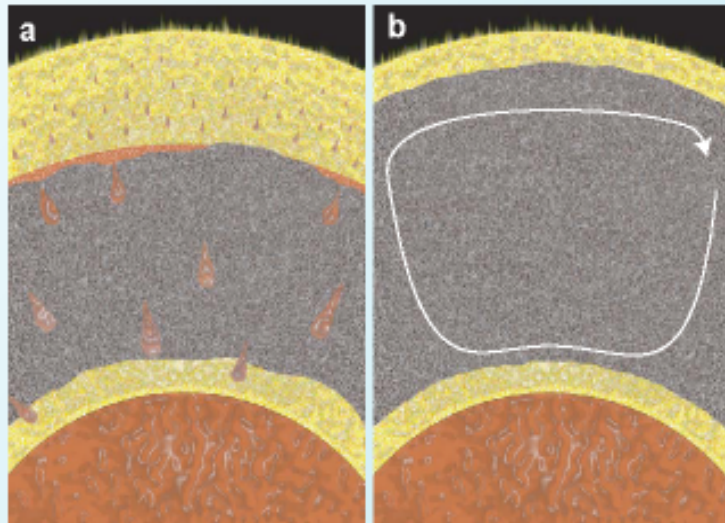
a: Percolation of iron by diapiric instabilities



Magma ocean model

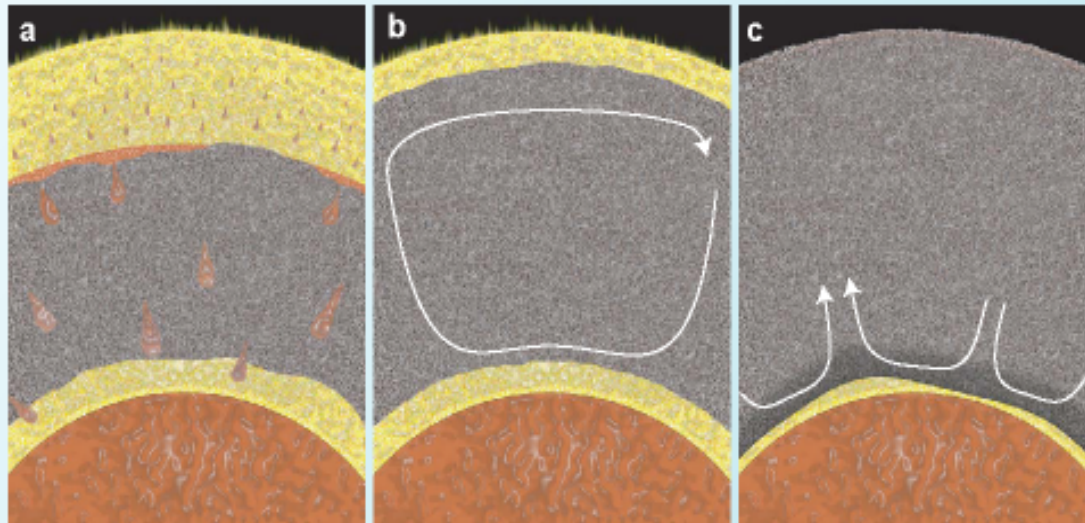
a: Percolation of iron by diapiric instabilities

b: Crystallisation from up and bottom with different rates



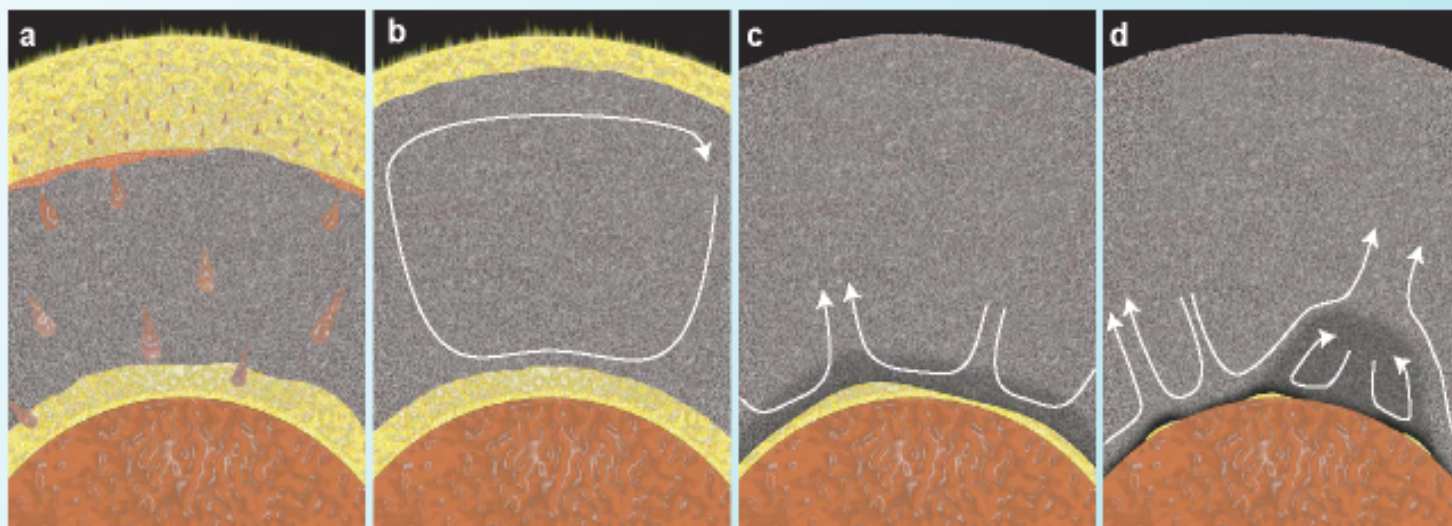
Magma ocean model

- a: Percolation of iron by diapiric instabilities
- b: Crystallisation from up and bottom with different rates
- c: Crystallisation of Fe-enriched solids



Magma ocean model

- a: Percolation of iron by diapiric instabilities
- b: Crystallisation from up and bottom with different rates
- c: Crystallisation of Fe-enriched solids
- d: Actual state with remaining mushy layer and partial melt



Stability of melt layer at the CMB

Gravitationnal stability :

- If enrichment in iron relative to magnesium
- If small or negative melting slope

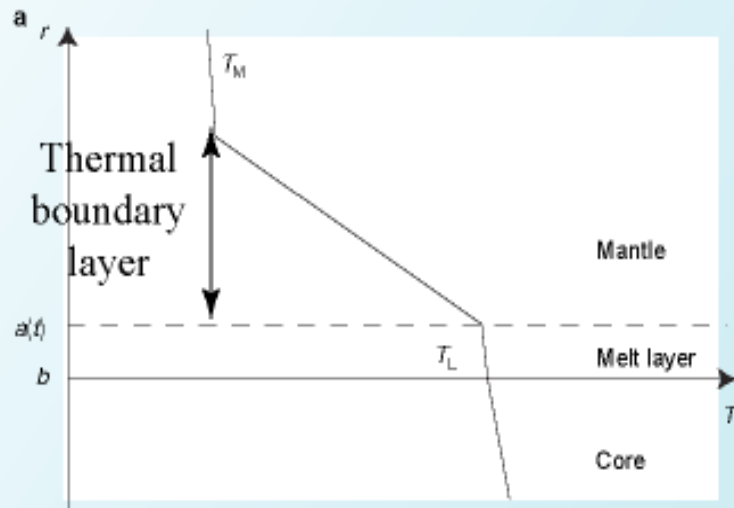
Chemical stability :

- If complete equilibrium with core, due to low viscosity
- Chemical interaction between core and mantle not well constrained

Evolution model of this melt layer

$$4\pi a^2 k \frac{T_L - T_M}{\delta} = - (M_m C_{pm} + M_C C_{pC}) \frac{dT_L}{dt} + H(t) - 4\pi a^2 \rho \Delta S T_L \frac{da}{dt}$$

Heat variation due to temperature variation in thermal boundary layer = - Specific heat production + Radiogenic heat production - Latent heat production

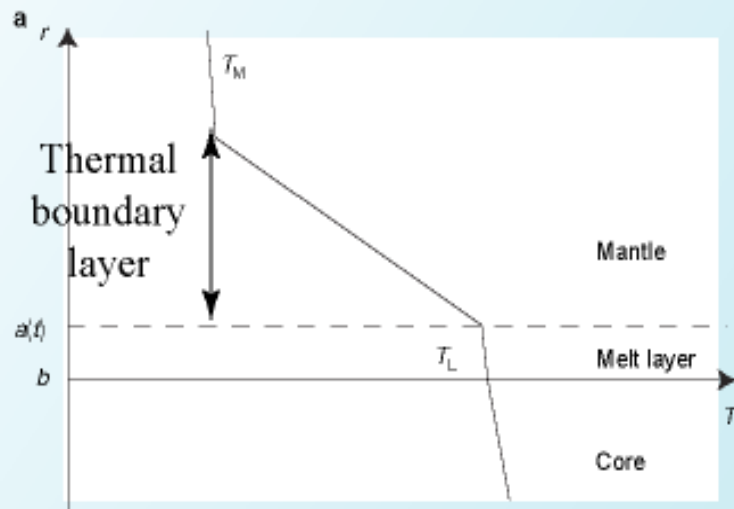


Adiabatic temperature gradient in melt layer and core

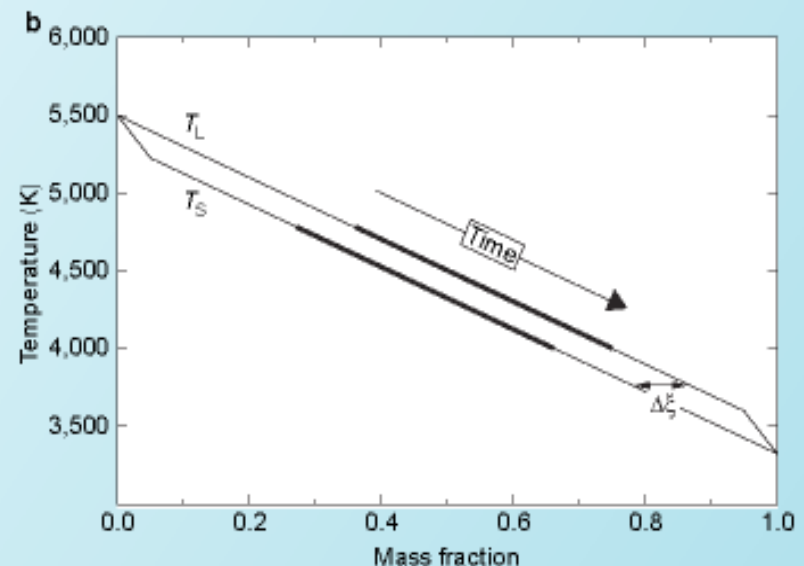
Evolution model of this melt layer

$$4\pi a^2 k \frac{T_L - T_M}{\delta} = - (M_m C_{pm} + M_c C_{pc}) \frac{dT_L}{dt} + H(t) - 4\pi a^2 \rho \Delta S T_L \frac{da}{dt}$$

$$\frac{d\xi_L}{dt} = - \frac{3a^2 \Delta \xi}{a^3 - b^3} \frac{da}{dt}$$



Adiabatic temperature gradient in melt layer and core

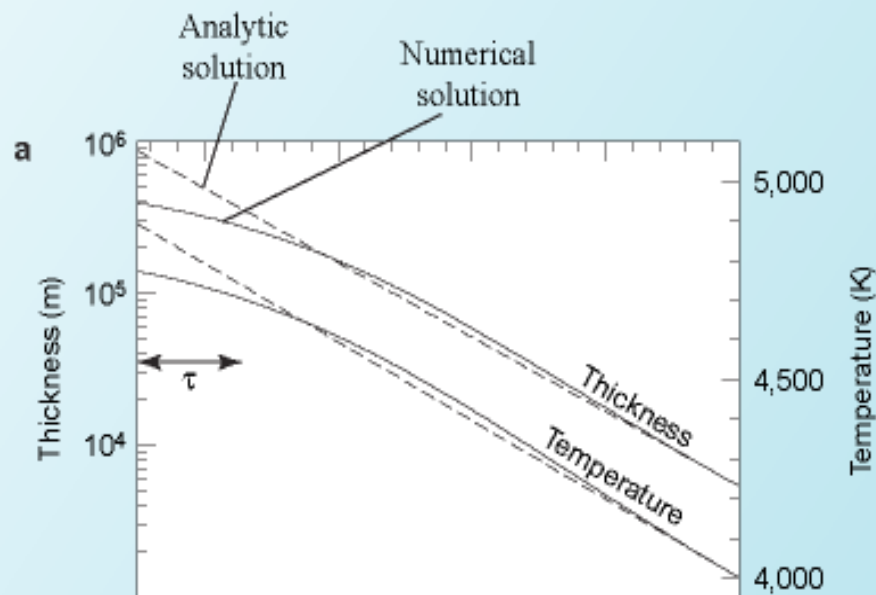


Idealized solid solution

Evolution model of this melt layer

$$4\pi a^2 k \frac{T_L - T_M}{\delta} = - (M_m C_{pm} + M_c C_{pc}) \frac{dT_L}{dt} + H(t) - 4\pi a^2 \rho \Delta S T_L \frac{da}{dt}$$

$$\frac{d\xi_L}{dt} = - \frac{3a^2 \Delta \xi}{a^3 - b^3} \frac{da}{dt}$$

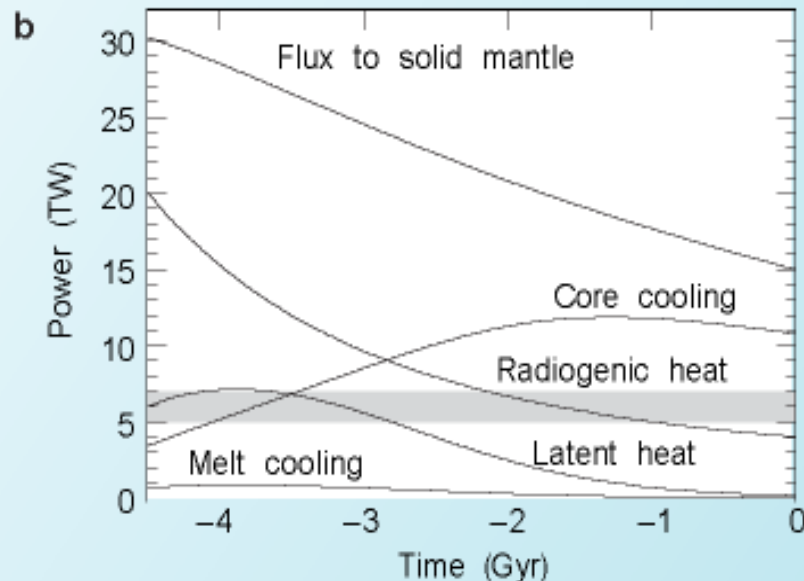


τ : e-fold time of decay of layer thickness : ~ 1 Gyr

Evolution model of this melt layer

$$4\pi a^2 k \frac{T_L - T_M}{\delta} = - (M_m C_{pm} + M_C C_{pC}) \frac{dT_L}{dt} + H(t) - 4\pi a^2 \rho \Delta S T_L \frac{da}{dt}$$

$$\frac{d\xi_L}{dt} = - \frac{3a^2 \Delta \xi}{a^3 - b^3} \frac{da}{dt}$$



Evolution of heat production with time

Generation of geodynamo

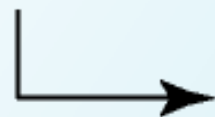
Due to thermal convection

No need of compositional convection for geodynamo

Melt layer at the CMB as hidden reservoir

Formed in the first 100 Myr of the Earth's history (as necessitated by $\epsilon^{142}\text{Nd}$)

Nb/Ta and Nb/La ratio of hidden reservoir must be higher than Earth

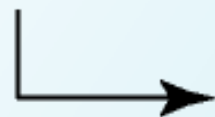


As Nb is more incompatible than Ta and La,
hidden reservoir must be derived from melt.

Melt layer at the CMB as hidden reservoir

Formed in the first 100 Myr of the Earth's history (as necessitated by $\epsilon^{142}\text{Nd}$)

Nb/Ta and Nb/La ratio of hidden reservoir must be higher than Earth



As Nb is more incompatible than Ta and La,
hidden reservoir must be derived from melt.

So basal magma ocean is a good candidate
for the hidden reservoir.

Evolution of isotopic composition of Earth and basal magma ocean

$$\frac{d}{dt} {}^{146}\text{Sm}_m = - {}^{146}\text{Sm}_m \lambda_{146} + {}^{146}\text{Sm}_m (D_{sm} - 1) \frac{1}{M_m} \frac{dM_m}{dt}; \quad (7)$$

$$\frac{d}{dt} {}^{142}\text{Nd}_m = {}^{146}\text{Sm}_m \lambda_{146} + {}^{142}\text{Nd}_m (D_{nd} - 1) \frac{1}{M_m} \frac{dM_m}{dt} \quad (8)$$

$$\frac{d}{dt} {}^{147}\text{Sm}_m = - {}^{147}\text{Sm}_m \lambda_{147} + {}^{147}\text{Sm}_m (D_{sm} - 1) \frac{1}{M_m} \frac{dM_m}{dt} \quad (9)$$

$$\frac{d}{dt} {}^{143}\text{Nd}_m = {}^{147}\text{Sm}_m \lambda_{147} + {}^{143}\text{Nd}_m (D_{nd} - 1) \frac{1}{M_m} \frac{dM_m}{dt} \quad (10)$$

$$\frac{d}{dt} {}^{144}\text{Nd}_m = {}^{144}\text{Nd}_m (D_{nd} - 1) \frac{1}{M_m} \frac{dM_m}{dt} \quad (11)$$

$$\frac{d}{dt} {}^{146}\text{Sm}_s = - {}^{146}\text{Sm}_s \lambda_{146} + ({}^{146}\text{Sm}_s - {}^{146}\text{Sm}_m D_{sm}) \frac{1}{M_s} \frac{dM_m}{dt}; \quad (12)$$

$$\frac{d}{dt} {}^{142}\text{Nd}_s = {}^{146}\text{Sm}_s \lambda_{146} + ({}^{142}\text{Nd}_s - {}^{142}\text{Nd}_m D_{nd}) \frac{1}{M_s} \frac{dM_m}{dt} \quad (13)$$

$$\frac{d}{dt} {}^{147}\text{Sm}_s = - {}^{147}\text{Sm}_s \lambda_{147} + ({}^{147}\text{Sm}_s - {}^{147}\text{Sm}_m D_{sm}) \frac{1}{M_s} \frac{dM_m}{dt} \quad (14)$$

$$\frac{d}{dt} {}^{143}\text{Nd}_s = {}^{147}\text{Sm}_s \lambda_{147} + ({}^{143}\text{Nd}_s - {}^{143}\text{Nd}_m D_{nd}) \frac{1}{M_s} \frac{dM_m}{dt} \quad (15)$$

$$\frac{d}{dt} {}^{144}\text{Nd}_s = ({}^{144}\text{Nd}_s - {}^{144}\text{Nd}_m D_{nd}) \frac{1}{M_s} \frac{dM_m}{dt}; \quad (16)$$

$$\frac{{}^{146}\text{Sm}_s}{{}^{144}\text{Nd}} = \frac{{}^{146}\text{Sm}_0}{{}^{144}\text{Nd}} e^{-\lambda_{146} t}; \quad (17)$$

$$\frac{{}^{147}\text{Sm}_s}{{}^{144}\text{Nd}} = \frac{{}^{147}\text{Sm}_0}{{}^{144}\text{Nd}} e^{-\lambda_{147} t}; \quad (18)$$

$$\frac{{}^{142}\text{Nd}_s}{{}^{144}\text{Nd}} = \frac{{}^{142}\text{Nd}_p}{{}^{144}\text{Nd}} - \frac{{}^{146}\text{Sm}_0}{{}^{144}\text{Nd}} e^{-\lambda_{146} t}; \quad (19)$$

$$\frac{{}^{143}\text{Nd}_s}{{}^{144}\text{Nd}} = \frac{{}^{143}\text{Nd}_p}{{}^{144}\text{Nd}} - \frac{{}^{147}\text{Sm}_0}{{}^{144}\text{Nd}} e^{-\lambda_{147} t}; \quad (20)$$

Evolution of not
fractionated standard

Mass balance equations for
each isotopes

Evolution of isotopic composition of Earth and basal magma ocean

$$Nd_{mi} = \frac{Nd_i}{D_{Nd}(1 - F) + F} \quad (21)$$

$$Sm_{mi} = \frac{Sm_i}{D_{Sm}(1 - F) + F} \quad (22)$$

$$Nd_{si} = \frac{Nd_i(M_{si} + M_{mi}) - Nd_{mi}M_{mi}}{M_{si}} \quad (23)$$

$$Sm_{si} = \frac{Sm_i(M_{si} + M_{mi}) - Sm_{mi}M_{mi}}{M_{si}} \quad (24)$$

Initial chemical composition of each reservoir

$$M_m = M_{mi}e^{-(t-t_i)/\tau} \quad (25)$$

Exponential decrease of melt layer mass

Evolution of isotopic composition of Earth and basal magma ocean

$$^{146}\text{Sm}_m = ^{146}\text{Sm}_{mi} e^{(\lambda_{146} + (D_{Sm} - 1)/\tau)(t - t_i)}; \quad (26)$$

$$^{147}\text{Sm}_m = ^{147}\text{Sm}_{mi} e^{(\lambda_{147} + (D_{Sm} - 1)/\tau)(t - t_i)}; \quad (27)$$

$$^{144}\text{Nd}_m = ^{144}\text{Nd}_{mi} e^{(1 - D_{Nd})(t - t_i)/\tau} \quad (28)$$

$$^{142}\text{Nd}_m = ^{142}\text{Nd}_{mi} e^{(1 - D_{Nd})(t - t_i)/\tau} \left[1 + \frac{^{146}\text{Sm}_{mi} \lambda_{146}}{^{142}\text{Nd}_{mi} (D_{Nd} - D_{Sm})} \frac{e^{(D_{Nd} - D_{Sm}) (t - t_i)/\tau} - 1}{\lambda_{146}} \right]; \quad (29)$$

$$^{143}\text{Nd}_m = ^{143}\text{Nd}_{mi} e^{(1 - D_{Nd})(t - t_i)/\tau} \left[1 + \frac{^{147}\text{Sm}_{mi} \lambda_{147}}{^{143}\text{Nd}_{mi} (D_{Nd} - D_{Sm})} \frac{e^{(D_{Nd} - D_{Sm}) (t - t_i)/\tau} - 1}{\lambda_{147}} \right]; \quad (30)$$

$$^{146}\text{Sm}_s = \frac{e^{-\lambda_{146}(t - t_i)}}{M_s} \left[^{146}\text{Sm}_i M_{tot} - ^{146}\text{Sm}_i M_m e^{(1 - D_{Sm})(t - t_i)/\tau} \right]; \quad (31)$$

$$^{147}\text{Sm}_s = \frac{e^{-\lambda_{147}(t - t_i)}}{M_s} \left[^{147}\text{Sm}_i M_{tot} - ^{147}\text{Sm}_i M_m e^{(1 - D_{Sm})(t - t_i)/\tau} \right]; \quad (32)$$

$$^{142}\text{Nd}_s = \frac{M_{tot}}{M_s} ^{142}\text{Nd}_i + \frac{^{146}\text{Sm}_i}{M_s} \left[1 - e^{-\lambda_{146}(t - t_i)} \right] \frac{M_m}{M_s} ^{142}\text{Nd}_m; \quad (33)$$

$$^{143}\text{Nd}_s = \frac{M_{tot}}{M_s} ^{143}\text{Nd}_i + \frac{^{147}\text{Sm}_i}{M_s} \left[1 - e^{-\lambda_{147}(t - t_i)} \right] \frac{M_m}{M_s} ^{143}\text{Nd}_m; \quad (34)$$

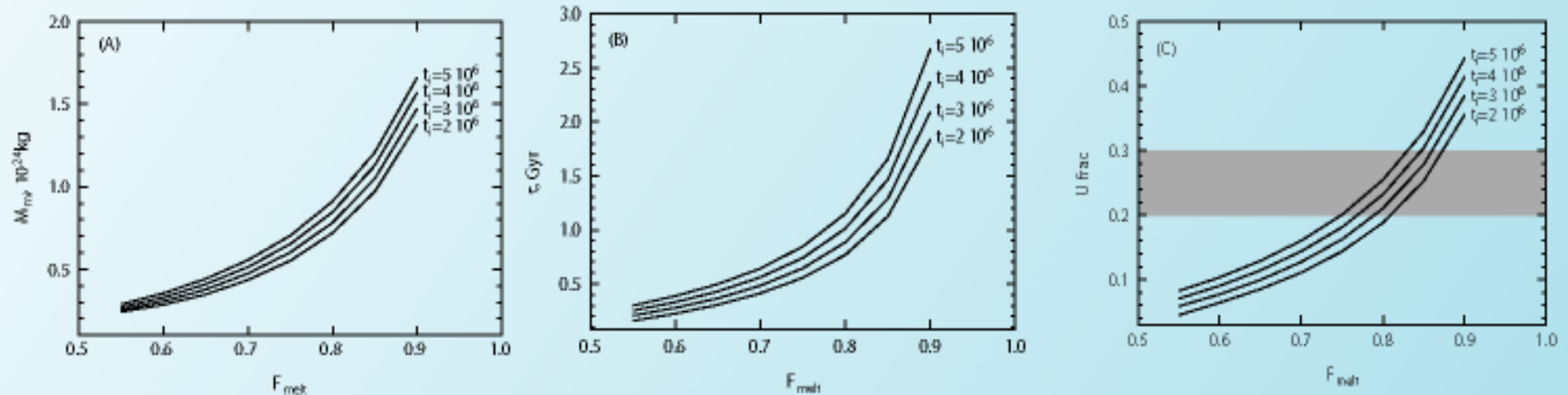
$$^{144}\text{Nd}_s = \frac{1}{M_s} \left[^{144}\text{Nd}_i M_{tot} - ^{144}\text{Nd}_m M_m \right]; \quad (35)$$

Final mass balances equations

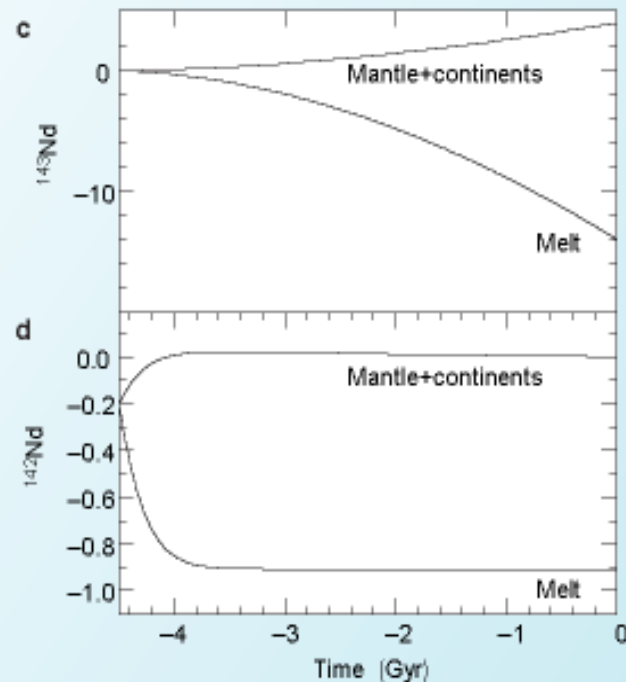
Evolution of isotopic composition of Earth and basal magma ocean

Four independent parameters :

- Initial mass of melt layer M_{mi}
- Its crystallisation time τ
- Its time of formation t_i
- Its melt fraction F



Evolution of isotopic composition of Earth and basal magma ocean



$F=80\%$ (corresponds to ~ 850 km thick)

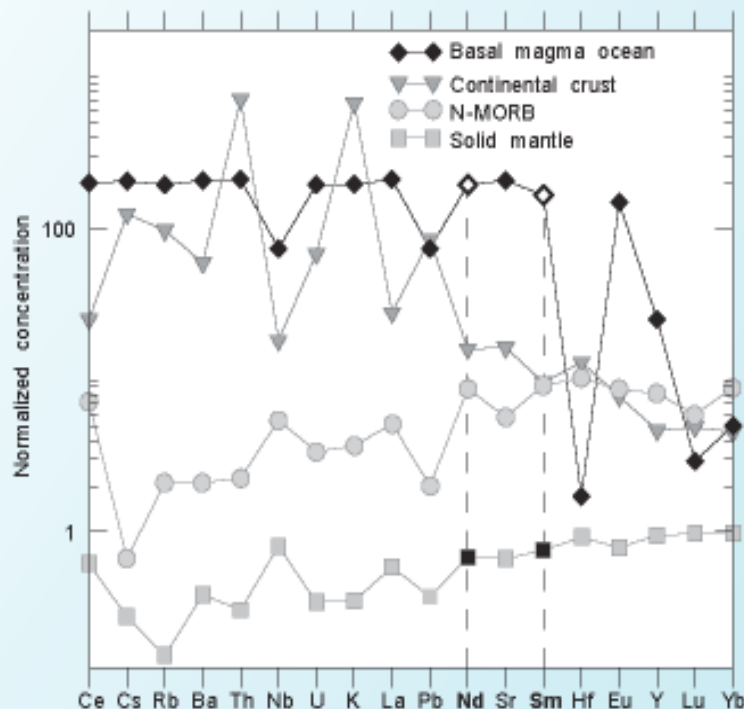
$M_{\text{mi}} = 0.78 \cdot 10^{24} \text{ kg}$

$\tau = 887 \text{ Myr}$

$t_i = 30 \text{ Myr}$

Good agreement with observed values

Predicted element concentration in present-day mantle and basal magma ocean

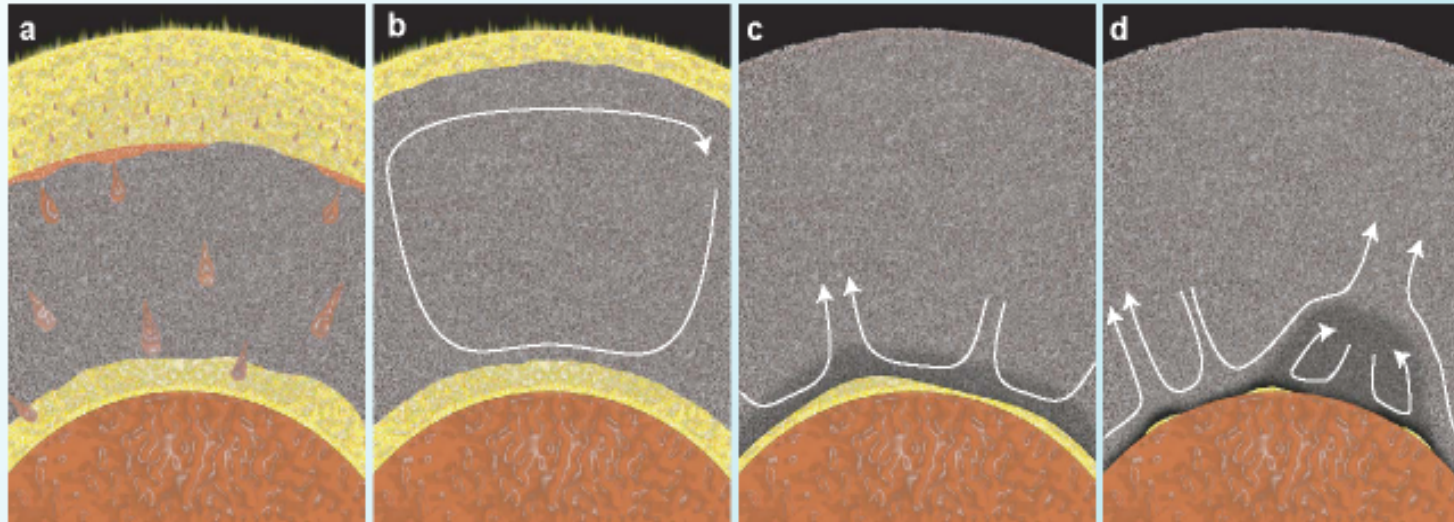


Calculation made by
applying a mass balance
between continental crust
and remaining melt.



A "continental crust-like" at
the top of the Earth's core

Magma ocean model



a : 850 km thick layer extracted by 80% of melting of lower mantle

b-c: Increasing Fe/Mg ratio with time in crystallising material due to magma differentiation

d: Denser piles accumulate under plume roots and incompatible elements are trapped in remaining melt